

Mathematics Problem of the Week (248)

This week's winner is:

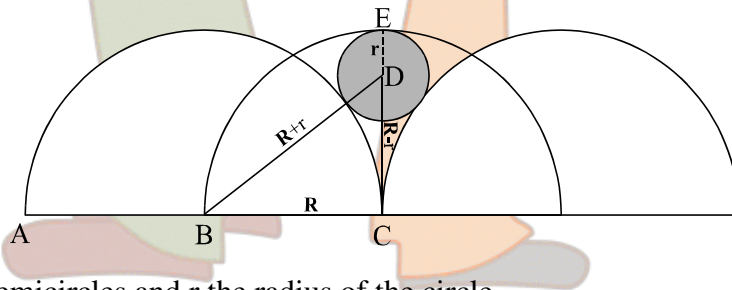
Brady Schmidt

Contact Lin Hammill (Surrey Fir 348) or Judy Bicep (Richmond,3335) for your prize or email MathProblem@kpu.ca.

Also submitting correct solutions to problem 248 were:

Anthony Roberts, Matt Potma, David Luna, and Suzanne Pearce

Problem 248 solution:



Let R be the radius of the semicircles and r the radius of the circle.

BC is the radius of a semicircle and so is of length R .

Then, since the circle and semicircles are tangent BD is a line segment with length $R+r$.

CE is the radius of the middle semicircle and so it is of length R . Since DE is of length r , CD is of length $R-r$.

Applying Pythagoras Theorem to triangle BCD we obtain:

$$\begin{aligned}R^2 + (R-r)^2 &= (R+r)^2 \\R^2 + R^2 - 2rR + r^2 &= R^2 + 2rR + r^2 \\R^2 &= 4rR \\R &= 4r\end{aligned}$$

Thus the ratio is $\frac{r}{R} = \frac{1}{4}$.