

## Useful Equations

$$\cos \alpha = \frac{A_x}{A} \quad \cos \beta = \frac{A_y}{A} \quad \cos \gamma = \frac{A_z}{A}$$

$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

$$F = ks \quad \sum \vec{F}_i = 0 \quad \sum \vec{M}_{O_i} = 0 \quad \hat{u} = \frac{\vec{R}}{|\vec{R}|}$$

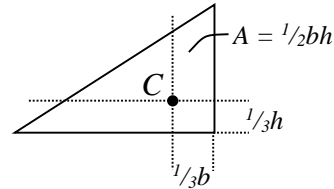
$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta = A_x B_x + A_y B_y + A_z B_z$$

$$\vec{F} = \vec{F}_{\parallel} + \vec{F}_{\perp} \quad \vec{M}_O = \vec{R}_{OF} \times \vec{F} = \begin{vmatrix} i & j & k \\ R_x & R_y & R_z \\ F_x & F_y & F_z \end{vmatrix}$$

$$M_u = \hat{u} \cdot (\vec{R}_{OF} \times \vec{F}) = \begin{vmatrix} u_x & u_y & u_z \\ R_x & R_y & R_z \\ F_x & F_y & F_z \end{vmatrix}$$

$$\vec{M}_{Couple} = \vec{d}_{\perp} \times \vec{F} \quad |\vec{R}| = \sqrt{R_x^2 + R_y^2 + R_z^2}$$

$$\bar{x} = \frac{\int_L xw(x) dx}{\int_L w(x) dx}$$



$$\sum_i \vec{F}_i = m\vec{a} \quad f_s^{Max} = \mu_s N \quad f_k = \mu_k N \quad y = (x \tan \theta) - \left( \frac{gx^2}{2v_0^2} \right) (1 + \tan^2 \theta)$$

$$v = \frac{ds}{dt}$$

$$a = \frac{dv}{dt}$$

$$a ds = v dv$$

$$\rho = \frac{\left[ 1 + \left( \frac{dy}{dx} \right)^2 \right]^{\frac{3}{2}}}{\left| \frac{d^2y}{dx^2} \right|}$$

$$ds = \sqrt{1 + \left( \frac{dy}{dx} \right)^2} dx$$

$$a_t = \dot{v}$$

$$a_n = \frac{v^2}{\rho}$$

$$\tan \theta = \frac{dy}{dx}$$

$$\vec{v} = \dot{r} \mathbf{u}_r + r \dot{\theta} \mathbf{u}_{\theta} + \dot{z} \mathbf{u}_z$$

$$\vec{a} = (\ddot{r} - r\dot{\theta}^2) \mathbf{u}_r + (r\ddot{\theta} + 2\dot{r}\dot{\theta}) \mathbf{u}_{\theta} + \ddot{z} \mathbf{u}_z$$

$$\tan \psi = \frac{r}{dr/d\theta}$$

$$\vec{r}_B = \vec{r}_A + \vec{r}_{B/A}$$

$$\vec{v}_B = \vec{v}_A + \vec{v}_{B/A}$$

$$\vec{a}_B = \vec{a}_A + \vec{a}_{B/A}$$

$$U = \int_{r_1}^{r_2} \vec{F} \cdot d\vec{r} = \int_{r_1}^{r_2} F \cos \theta dr$$

$$U = F \Delta s \cos \theta$$

$$\frac{1}{2} m v_1^2 + \sum \int_{s_1}^{s_2} F ds = \frac{1}{2} m v_2^2$$

$$T = \frac{1}{2} m v^2$$

$$T_1 + U_{Total} = T_2$$

$$T_1 + V_1 + U_{nonconservative} = T_2 + V_2$$

$$V_{spring} = \frac{1}{2} k s^2$$

$$V_{gravity} = -\frac{GMm}{r}$$

$$V_{gravity} = mgh$$

$$\varepsilon = \frac{\text{Power output}}{\text{Power input}}$$

$$P = \frac{dU}{dt} = \vec{F} \cdot \vec{v}$$

$$\vec{L} = m\vec{v}$$

$$\vec{I} = \int_{t_1}^{t_2} \vec{F} dt = \Delta \vec{L}$$

$$m\vec{v}_i + \sum \int_{t_1}^{t_2} \vec{F}_i dt = m\vec{v}_f$$

$$m_1 \vec{v}_{1i} + m_2 \vec{v}_{2i} = m_1 \vec{v}_{1f} + m_2 \vec{v}_{2f}$$

$$e = -\frac{v_{Bf} - v_{Af}}{v_{Bi} - v_{Ai}}$$

$$\begin{pmatrix} v'_{xi} \\ v'_{yi} \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} v_x \\ v_y \end{pmatrix}$$

$$\begin{pmatrix} v_{xf} \\ v_{yf} \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} v'_{xf} \\ v'_{yf} \end{pmatrix}$$

$$\vec{H}_0 = \vec{r} \times m\vec{v}$$

$$(\vec{H}_0)_1 + \sum \int_{t_1}^{t_2} \vec{M}_0 dt = (\vec{H}_0)_2$$

$$\frac{dx^n}{dx} = nx^{n-1} \quad \frac{d}{dx} \tan x = \frac{1}{\cos^2 x} \quad \frac{d}{dx} \sin x = \cos x \quad \frac{d}{dx} \cos x = -\sin x \quad \frac{d}{dx} \ln x = \frac{1}{x}$$

$$\frac{df}{d\theta} = \frac{df}{dx} \frac{dx}{d\theta}$$